

非平衡态物理和计算方法

极端条件下的物态演化



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The Challenge of HEDP

The National Academy of Science report called the frontiers in High Energy Density Physics the X-Games of contemporary science



Z-pin experiments



激光产生温稠密物质动态演化



Laser induced the formation of warm dense matter: *Non-equilibrium process Ultrafast dynamics*

Ernstorfer et al. Science 323, 1033-1037 (2009)



Properties of HEDP

Plasmas consist of mobile charged particles (ions, electrons,..) interacting by long-range Coulombic N-body forces



Our understanding of plasma behavior in each of these regimes differs widely

Matter in the plasma state exists in an unimaginable variety



 $1 \,\text{eV} = 1.16 \times 10^4 \,\text{K}$

Properties of HEDP

Matter under high energy density conditions, exhibits complex behavior not typically associated with classical plasmas



Properties of HEUP

An ICF example: Spanning strongly coupled (large particle-particle correlations) to weakly coupled (Brownian motion like) regimes

Weakly coupled plasma: $\Gamma << 1$

- Collisions are long range and many body
- Weak ion-ion and electron-ion correlations
- Debye sphere is densely populated
- Kinetics is the result of the cumulative effect of many small angle weak collisions
- Theory is well developed $1/n\lambda_D^3 << 1$

Strongly coupled plasma: $\Gamma \ge 1$

- Large ion-ion and electron-ion correlations
- Particle motions are strongly influenced by nearest neighbor interactions
- Debye sphere is sparsely populated
- Large angle scattering as the result of a single encounter becomes important



density-temperature trajectory of the DT gas in an ICF capsule

Multi-scale challenge

The multi-scale problem: Applications require simulation at the macroscale but need fundamental physics information from the micro-scale



Multi-scale challenge

The multi-scale problem: Applications require simulation at the macroscale but need fundamental physics information from the micro-scale



Why is matter in the high energy density regime so interesting: The hot dense matter regime



Kremp et al., "Quantum Statistics of Non-ideal Plasmas", Springer-Verlag (2005)

Drivers for Hot Dense Matter research

What are the major challenges facing each of the critical areas of hot dense matter ?

Thermonuclear burn

Particle spectra (do D and T distributions remain Maxwellian?) Electron, ion and radiation T(t) The role of high Z impurities

Equations of state

Thermal conductivity Species diffusivity

Transport properties of hot dense matter

Thermal conductivity Species diffusivity The role of high Z impurities

Momentum and energy exchange rates

Stopping power Electron ion coupling The role of high Z impurities



Comprehensive theory describing hot dense matter plasmas with impurities

Strongly coupled high Z component and weakly coupled low Z component

The challenge of WDM

Warm dense matter regime is at the meeting point of several distinct physical regimes- a scientifically rich area of HEDP



"Warm dense matter (WDM) is an intermediate state between condensed matter (solids and liquids), gases, and ideal plasmas. It exists in the lower-temperature portion of the HED regime, under conditions where the assumptions of both condensed-matter theory and ideal-plasma theory break down, and where quantum mechanics, particle correlations, and electric forces are all important."



The WDM challenge: Well developed models when extended to WDM face severe problems





Matter in the plasma state exists in an unimaginable variety



 $1 \,\text{eV} = 1.16 \times 10^4 \,\text{K}$



From single atomic model to strongly coupled ions



- 1. Interionic interaction potential in HDM with large excitations and ionizations of electrons
- 2. Simulations of the atomic thermomotions
- 3. Microfield distributions





Drivers for WDM research

What are the major challenges facing each of the critical areas of warm dense matter ?

Phase Transitions in WDM

Melting, liquid-liquid phase transitions, plasma phase transitions Metal-insulator transition

Equations of state and their dependence on formation history Computation of EOS without decomposition of ionic and electronic contributions EOS for mixtures

Transport properties of WDM Viscosity, diffusivity, electric, ionic and thermal conductivity

Constitutive properties of warm solids

What is a solid at very high pressures?

Deformation and dissipation mechanisms (strength)

Comprehensive theory connecting WDM regions

DFT: Orbital-free, exact exchange, going beyond Born-Oppenheimer, high B fields Particle simulation methods

What are the key questions in dense matter?

Simulations predict electronic localization through compression

How does chemistry change at extreme densitie

How do core electrons affect bonding? What is the nature of insulator-metal transitions at high

What is a solid at > 10 Mbar?

How do melt, strength, structure, EOS change at ultra-h How fast can you squish a solid?

What is the nature of He or H when the interaton ncreasing ~deBroglie wavelength?

How do mixtures of H and He behave at high densities?



Compression

Neil Ashcroft, 2010





随着强激光技术的发展和应用,以美国的国家点火装置和 我国的点火计划为代表,有可能在实验室制备这种极端物态, 甚至创造以空心原子、电子泡为代表的新物质,探索激光聚 变等新能源技术和太赫兹与阿秒脉冲等新光源。





精密计算物性参数
统一描述临界状态
实时诊断超快过程

核武器精密化设计和新型能源开发
极端条件下材料应用
超快电子信息器件研发

需要构建基于离子间相互 作为基础的**多尺度模拟**方 法,对涉及到的**跨尺度问** 题进行直接模拟和物理效 应研究 **宏观尺度** (连续) 计算粗粒度场变量 $n_e^{cg}(\mathbf{r})$ 和 $\Phi^{cg}(\mathbf{r})$

微观尺度
 (原子内)
 分离自由态和束缚态,
 指定电荷数 Z^{*}_i, 并构
 造 ρ_{ion}(**r**)。

介观尺度 (离子间) 计算有效相互作用,根 据受力更新电子位置。



- First principles based on quantum mechanics: DFT, QMC, Hartree-Fock, Field Theory..... Advantage—Accuracy
- Semiclassical Method: averaged atoms model, MD based on empirical interatomic potential, (electron) force field.....
 - Advantage—Largescale, dynamics

Fe phase - Conditions under (super) earth core

PRL 108, 055505 (2012)

PHYSICAL REVIEW LETTERS

week ending 3 FEBRUARY 2012



What pressures-temperatures can you achieve with drivers ?



Hicks, 2006

High pressure phases of aluminum are also predicted to be complex



lons in a "Sea of Hot Electrons"



动力学碰撞——非绝热效应

分子动力学方法

• 分子动力学方法

基本思想:物质是由原子和分子组成的多粒子系统, 假定粒子在由经典力学描述的特定轨道上运动,计算 粒子受到的作用力,求解运动方程得到系统中全体粒 子在相空间中的运动轨迹,进而计算系统的热力学参 数和输运性质。

基本假设:各态历经假设

粒子为经典粒子

分子动力学方法

• 分子动力学方法

核心问题:1. 计算原子间相互作用势 2. 积分牛顿运动方程

> 限制: 有限观测时间 有限系统大小

 [1] M. P. Allen, D. J. Tildesley, Computer Simulation of Liquids (1987)
 [2] Frenkel & Smit, Understanding Molecular Simulation—From Algorithms to Applications (1996)



A key concept to understand material properties

- Born-Oppenheimer Approximation
- Propagation of the nuclei on the potential energy surface (PES)
- Most popular method: *ab initio* MD



Brownian Motion: Langevin Equation



A large Brownian particle with mass M immersed in a fluid of much smaller and lighter particles.

激光产生温稠密物质动态演化

- Non-adiabatic effects: excitation, transition, collisions et al.
- Electron-ion collisions induced friction (EI-CIF)
- Langevin Equation:

DFT

$$M_I \ddot{\boldsymbol{R}}_I = \boldsymbol{F} - \gamma M_I \dot{\boldsymbol{R}}_I + N_I$$

Friction White coefficient noise

EOS and electronic structures up to 100 eV can be studied.

Dai and Yuan*. Phys. Rev. Lett. 104: 245001 (2010); Phys. Rev. Lett. 109: 175701 (2012)

L. G. Stanton et al. Pys. Rev. X 8, 021044 (2018);

Kang and Dai*. J. Phys.: Condens. Matter 30, 073002 (2018) (Topic Review).

QLMD

Hugoniot: data from QLMD



Hugoniot: structures from QLMD



$$ECN = rac{1}{N}\sum_{i=1}^{N}ECN_i = rac{1}{N}\sum_{i=1}^{N}\sum_{j
eq i}\exp\left[1-\left(rac{d_{ij}}{d_{av}^i}
ight)^6
ight]$$

"effective coordination numbers" (ECN)

$$d_{av}^{i} = \frac{\sum_{j} d_{ij} \exp\left[1 - \left(\frac{d_{ij}}{d_{av}^{i}}\right)^{6}\right]}{\sum_{j} \exp\left[1 - \left(\frac{d_{ij}}{d_{av}^{i}}\right)^{6}\right]}, d_{av} = \frac{1}{N} \sum_{i=1}^{N} d_{av}^{i}$$

Temperature effect--lonic short ordered structures



There are medium or short ordered structures in hot dense matter

Dai Jiayu et al. HEDP, 7: 84-90 (2011)



lonic structures




lonic structures



T = 100 eV ρ= 33.385 g/ccm

Temperature effect- - Dynamical ionic clusters with flowing electron bubbles





Electronic bubbles



×



Dyugaey [J. Low Temp. Phys. 78, 79 (1990)]:

(1) exchange of particles is negligible (Boltzmann statistics), but the quantum delocalization effects are still relevant

$$\lambda < d$$
 or $\lambda \sim d$

② exchange of particles is relevant and Bose-Einstein or Fermi-Dirac statistics should be applied

$$\lambda >> d$$



Quantum effect of ions in dense matter

1 eV
$$\lambda = \frac{h}{\sqrt{2\pi m k_B T}} = \frac{\sqrt{2\pi}}{\sqrt{1836 \times \frac{1}{27.21}}} a.u. \approx 0.305 a.u. = 0.16 \dot{A}$$
1 g/cm³
$$d = \sqrt[3]{\frac{m}{\rho}} = \sqrt[3]{\frac{\frac{1}{6.02 \times 10^{23} \, g}}{1.0 g \, / \, cm^3}} \approx 1.18 \dot{A}$$

10 g/cm³

$$d = \sqrt[3]{\frac{m}{\rho}} = \sqrt[3]{\frac{\frac{1}{6.02 \times 10^{23} g}}{10 g / cm^3}} \approx 0.55 \dot{A}$$

Path integral molecular dynamics:



Nuclear quantum effects—path integral molecular dynamics



The *N*-particle quantum system is isomorphic to a *N* interacting ring polymers of length *P* with harmonic intrapolymeric forces.



bead

spring



离子的量子效应



路径积分分子动力学方法

• 路径积分

$$K(x,t;x_0,t_0) = \sum_{x(t)} a \exp\left(\frac{i}{\hbar} I[x(t)]\right) = \int \exp\left(\frac{i}{\hbar} I[x(t)]\right) Dx(t)$$

$$I[x(t)] = \int_{t_0}^t L(x, \dot{x}) dt$$

- 当 *I* >> ħ 时,使泛涵I [x(t)] 取极值的
 路径 x_c(t)邻近的路径的贡献不可忽略
- 当二者可比拟时,必须考虑所有路径的 贡献



路径积分分子动力学方法

处于热力学平衡状态的量子系统可以处于各种不同的能级,系统处于能量为 E_i 的状态的几率正比于 $exp(-\beta E_i)$

$$P_{i} = \frac{1}{Z} \exp(-\beta E_{i}) \qquad \sum_{i} P_{i} = 1 \qquad \beta = \frac{1}{k_{B}T}$$
$$Z = \sum_{i} \exp(-\beta E_{i})$$

密度矩阵
$$\rho(x_2, x_1) = \sum_i \phi_i(x_2) \phi_i^*(x_1) \exp(-\beta E_i) = \exp(-\beta H)$$

配分函数 $Z = Tr(\rho) = \int \rho(x, x) dx$

路径积分分子动力学方法

密度矩阵
$$\rho(x_2, x_1) = \sum_i \phi_i(x_2) \phi_i^*(x_1) \exp(-\beta E_i)$$

传播函数 $K(x_2, t_2; x_1, t_1) = \sum_i \phi_i(x_2) \phi_i^*(x_1) \exp\left(-\frac{i}{\hbar} E_i(t_2 - t_1)\right)$

$$\rho(x_2, x_1)$$
可用 $K(x_2, t_2; x_1, t_1)$ 路径积分的方法计算

$$t_2 - t_1 \rightarrow -i\beta\hbar$$
 $u = it$ $u_2 = \hbar\beta, u_1 = 0$

$$\rho(x_2, x_1) = \int \exp\left\{-\frac{1}{\hbar} \int_{0}^{\beta\hbar} \left[\frac{m}{2} \dot{x}^2(u) + V(x)\right] du\right\} Dx(u)$$

$$Z = \int \rho(x, x) dx = \int dx_1 \int_{x_1}^{x_1} \exp\left\{-\frac{1}{\hbar} \int_{0}^{\beta\hbar} \left[\frac{m}{2} \dot{x}^2(u) + V[x(u)]\right] du\right\} Dx(u)$$

$$Z = \int \rho(x, x) dx = \int dx_1 \int_{x_1}^{x_1} \exp\left\{-\frac{1}{\hbar} \int_{0}^{\beta\hbar} \left[\frac{m}{2} \dot{x}^2(u) + V[x(u)]\right] du\right\} Dx(u)$$

$$u$$
 "时间" $\dot{x} = \frac{dx}{du}$ "速度" $\frac{m}{2}\dot{x}^2$ "动能"

离散化:

$$Z = \int \rho(x, x) dx = \int dx_1 \left\langle x_1 \left| e^{-\beta(T+U)} \right| x_1 \right\rangle = \lim_{P \to \infty} \int dx_1 \left\langle x_1 \left| \Omega^P \right| x_1 \right\rangle$$
$$\Omega = e^{-\frac{\beta}{2P}U} e^{-\frac{\beta}{P}T} e^{-\frac{\beta}{2P}U}$$

Trotter theorem:
$$e^{\alpha(A+B)} = \lim_{P \to \infty} \left[e^{\frac{\alpha}{2P}B} e^{\frac{\alpha}{P}A} e^{\frac{\alpha}{2P}B} \right]^P$$

$$\begin{split} \mathbf{B} \langle \mathbf{E} \langle \mathbf{R} \rangle \langle \mathbf{h} \rangle \langle \mathbf{r} \rangle \langle \mathbf{h} \rangle \langle \mathbf{h$$

路径积分分子动力学方法

Primitive variables $\{R_I\}^{(s)}$ \implies Normal mode variables $\{y_I\}^{(s)}$ $R_{I}^{(s)} = \sum_{i=1}^{P} a_{I}^{(k)} e^{2\pi i (s-1)(k-1)/P}$ $\begin{cases} y_{I}^{(s)} = \frac{1}{\sqrt{P}} \sum_{r=1}^{P} U_{sr} R_{I}^{(r)} \end{cases}$ $y_{I}^{(1)} = a_{I}^{(1)}$ $y_I^{(P)} = a_I^{((P+2)/2)}$ $y_{I}^{(2s-2)} = \text{Re}(a_{I}^{(s)})$ $y_{I}^{(2s-1)} = \text{Im}(a_{I}^{(s)})$ classical $y_I^{(1)} = R_I^c = \frac{1}{P} \sum_{P}^{P} R_I^{(r)}$ Centroid of the path 运动方程: $M_I^{\prime(s)}\ddot{y}_I^{(s)} = -\frac{1}{P}\frac{\partial E_0}{\partial v^{(s)}} - M_I^{(s)}\omega_p^2 y_I^{(s)}$ path integral quantum

路径积分分子动力学方法

总能量:
$$E = -\frac{\partial}{\partial \beta} \ln Z = \lim_{P \to \infty} \langle \varepsilon_P \rangle_{PI}$$

$$\varepsilon_{P} = \frac{3}{2} NPkT - \sum_{s=1}^{P} \sum_{I=1}^{N} \frac{1}{2} M_{I} \omega_{P}^{2} \left(R_{I}^{(s)} - R_{I}^{(s+1)} \right)^{2} + \frac{1}{P} \sum_{s=1}^{P} E_{0} \left(\left\{ R_{I} \right\}^{(s)} \right)$$

压强:
$$P = -\frac{1}{\beta} \frac{\partial}{\partial V} \ln Z = \lim_{P \to \infty} \langle P_P \rangle_{PI}$$

$$P_{P} = \frac{NP}{\beta V} - \frac{1}{3V} \sum_{s=1}^{P} \sum_{I=1}^{N} \left[M_{I} \omega_{p}^{2} \left(R_{I}^{(s)} - R_{I}^{(s+1)} \right)^{2} - \frac{1}{P} R_{I}^{(s)} \cdot \frac{\partial E_{0}}{\partial R_{I}^{(s)}} \right]$$

路径积分分子动力学方法

Centroid molecular dynamics (CMD)

Centroid trajectories of a quantum particle are generated by the semiclassical equation of motion

$$M_I \ddot{R}_I(t) = \left\langle F_I(R_1^C, \cdots, R_N^C) \right\rangle_{PI}$$
$$F_I(R_1^C, \cdots, R_N^C) = \sum_{s=1}^P f_I^{(s)}$$



运动方程:
$$M_I^{\prime(1)}\ddot{y}_I^{(1)} = -\frac{1}{P}\frac{\partial E_0}{\partial y_I^{(1)}}$$
 $y_I^{(1)} = R_I^c = \frac{1}{P}\sum_{r=1}^P R_I^{(r)}$
 $M_I^{\prime(s)}\ddot{y}_I^{(s)} = -\frac{1}{P}\frac{\partial E_0}{\partial y_I^{(s)}} - M_I^{(s)}\omega_p^2 y_I^{(s)}$ $s = 2, \cdots, P$

绝热参数 γ

$$M_I^{\prime(1)} = M_I$$
$$M_I^{\prime(s)} = \gamma M_I^{(s)}$$

 $0 < \gamma < 1$

J. Chem. Phys. 101, 6168 (1994); Comput. Phys. Commun. 118, 166 (1999)







 $\omega_P = \sqrt{P}k_B T = \frac{2N}{g}\sqrt{P}E_0$

$$\omega_P(t) = \frac{2N}{g} \sqrt{P} (aE(t) + bE_0)$$

参数a和b通过两个条件确定:

1. 当
$$E(t) = E_0$$
时, $\omega_P = \frac{2N}{g}\sqrt{P}E_0$

2. 当 E(t) = 0 时, ω_p 达到最小 值, 使得环形分子的均方回转直径 等于德布罗意波长

$$a = 1 - (2R_{g0} / \lambda)^2$$
 $b = (2R_{g0} / \lambda)^2$





粒子量子隧穿的路径积分分子动力学

一维量子粒子势垒隧穿







离子的量子隧穿效应





Rev. Mod. Phys. 84, 1607 (2012)







- DFT with PBE exchange-correlation potential was used.
- Ultrasoft pseudopotential was used to describe the interaction between valence and core electrons.
- The plane-wave energy cutoff of 50 Ry was adopted with the charge-density cutoff of 400 Ry.
- Grimme scheme was used to treat van der Waals interaction.
- > The cubic supercell includes 16 water molecules.
- All MD and PIMD simulations were performed with modified Quantum-ESPRESSO package.

Ice X





NQEs on phase transition of high-pressure ice







NQEs on phase transition of high-pressure ice



61.2 GPa







NQEs on phase transition of high-pressure ice





Distributions of the O-H bond lengths at different pressures and temperatures

Free energy profiles of the protons along the two nearest neighbouring oxygen atoms obtained from quantum (solid lines) and classical (dashed lines) simulations.

Free energy profile: $\Delta F = -k_B T \ln[P(\delta)]$ $\delta = d(O_1H) - d(O_2H)$







Theory: Chem. Phys. Lett. 499, 236 (2010); Expt.: Phys. Rev. B 68, 014106 (2003)



K-edge x-ray absorption is an important probe of microscopic structure in high-pressure ice

- We use the full core hole approach to calculate the oxygen K-edge XAS of ice.
- DFT with PBE exchange-correlation potential
- We adopted a 4×4×4 k-points grid and a 90 Ry plane-wave energy cutoff to ensure the convergence.
- The calculated spectra were broadened using a Gaussian convolution of width 0.3 eV.
- The size of supercell including 16 water molecules is big enough for obtaining reliable oxygen K edge, as shown in the right figure.

D. Kang et al. Scientific Reports 3, 3272 (2013)



高压冰的相变和K边X射线吸收谱



Exp.: J. Phys. Chem. B 114, 3804 (2010)





自扩散系数与粘滞系数



Quantum effect of ions in dense matter



不同温度的10g/cm3氢的径向分布函数

不同温度的10g/cm3氢的电子压强、离子压强、 总压强



原子构型的演化





电子结构的演化



硅团簇的电子能级图。理论计算是采 用黑格尔(Hückol)近似并取团簇有一 定结构。



她治激发金团簇的电子激发模式



arXiv:2003.11191 67

 $p \sim N^{0.676 (\pm 0.034)}$

Au₂₅₀₀₀

10

Regime 3

9

 Au_{4200}

8

Au₇₀₀₀₀

11

12

Real time TD-DFT basis

Time dependent Schrödinger Equation

$$i\frac{\partial\psi(\mathbf{r},t)}{\partial t} = \hat{H}(\mathbf{r},t)\psi(\mathbf{r},t)$$

Time dependent wave function

$$\psi(\mathbf{r},t) = \sum_{i} c_i(t)\varphi_i(\mathbf{r},t)$$

Time dependent spin orbitals

$$|\varphi_i(\mathbf{r},t)
angle = \sum_{\mu} c_{\mu i}(t) |\chi_{\mu}(\mathbf{r})
angle$$

含时密度泛函理论(TDDFT)考虑

$$H\left(t, R_{j}(t), n(t)\right)\psi_{i}(t) = i\frac{\partial\psi_{i}(t)}{\partial t}$$



0 Energy (eV)





Au团簇的几何结构特点与吸收谱



Ν	Bulk	561	309	147	55	13	
d ^{core} (Å)	2.935	2.910	2.900	2.894	2.863	2.831	
$d_{av}^{surf}(\text{\AA})$	2.935	2.884	2.877	2.871	2.855	2.831	70

弱场下的电子电荷密度振荡



判断激发是单电子还是集体激发


激光激发金团簇的电子激发模式

场强增强引起Au团簇激发模式转变





流体模拟表明,是否考虑电子动力学对激光 和带电粒子能量沉积效率的影响达到50%

S. Hu, Phys. Rev. E 84, 016408 (2011) Collins et al. Phys. Rev. Lett. 121, 145001 (2018)

激光激发金团簇的电子激发模式

场强增强会导致单电子激发转变为集体激发



arXiv:2003.11191 (2020)

Accepted by National Science Review



Laser induced the formation of warm dense matter: *Non-equilibrium process Ultrafast dynamics*

Ernstorfer et al. Science 323, 1033-1037 (2009)



Kinetics model :

.

Temperature relaxation rate: Laudau-Spitzer theory

$$\nu_{ei} = \frac{8\sqrt{2\pi}n_i e^4 Z^2}{3mM} (\frac{k_B T_e}{m} + \frac{k_B T_i}{M})^{-3/2} ln\Lambda,$$

binary collisions, weakly coupled, dilute gases

Coulomb logarithm $ln\Lambda$

Lenard-Balescu (LB) (A. Lenard, Ann. Phys. (N.Y.) 10, 390 (1960).) Brown, Preston, and Singleton (BPS) (L. S. Brown, D. L. Preston, and R. L. Singleton, Phys. Rev. E 86, 016406 (2012).) Gericke, Murillo, and Schlanges (GMS) (D. O. Gericke, M. S. Murillo, and M. Schlanges, Phys. Rev. E 65, 036418 (2002).)

The general physics is to determine the cross sections

Molecular dynamics can also simulate the cross section



High Energy Density Physics 13 (2014) 34-39

Quantum statistical potential (QSP)

$$V_{ab}(r) = \frac{Z_a Z_b e^2}{r} \left[1 - \exp(-2\pi/\Lambda_{ab}) \right] + k_B T \ln 2\exp(-4\pi r^2 / (\Lambda_{ab}^2 \ln 2)) \delta_{ae} \delta_{be}$$

Classical MD:

- 1. Ion is treated as positive point charge
- 2. Electron is treated as negative point charge

Difficulties :

- 1. How to describe ionization and recombination
- 2. Coulomb Catastrophe
- 3. Quantum Scattering/cross sections

Quantum dynamics



Non-Born-Oppenheimer

Real dynamics and Large-scale simulation

Electron force field (eFF) MD

激光产生温稠密物质动态演化

Difficulties :

- 1. How to describe ionization and recombination
- 2. Coulomb Catastrophe
- 3. Quantum Scattering/cross sections

eFF can be viewed as an development of wave packet molecular dynamics considering electronic quantum effects and can describe non-adiabatic dynamics.



Assumption:

• Electrons are treated as Gaussian wave packets Ions are treated as charged points The collisions between electrons and ions are included naturelly

Gaussian wave packets:
$$\psi(\vec{r}) = (\frac{2}{\pi s^2})^{3/4} \exp[-(\frac{1}{s^2} - \frac{2p_s}{s}\frac{i}{\hbar})(\vec{r} - \vec{x})^2] \exp[\frac{i}{\hbar}\vec{p}_x \cdot \vec{r}]$$

Equation of motion:

$$\vec{p}_x = -\nabla_x V \vec{x} = \vec{p}_x / m_e$$

$$\dot{p}_{s} = -\partial V / \partial s$$

$$\dot{s} = (3m_{e} / 4)^{-1} p_{s}$$

$$\dot{\bar{p}}_{R} = -\nabla_{R} V$$

$$\bar{\bar{R}} = \bar{p}_{R} / m_{nuc}$$

 $=-\nabla_{R}V$

Electron Force Field method

Energy :

$$E = E_{eke} + E_{nuc \cdot nuc} + E_{nuc \cdot elec} + E_{elec \cdot elec} + E_{Pauli} + \sum_{i} \frac{1}{2} m_{e} \left| \dot{x}_{i} \right|^{2} + \frac{1}{2} (\frac{3}{4} m_{e}) \dot{s}_{i}^{2} + \sum_{j} \frac{1}{2} m_{ion} \left| \dot{x}_{j} \right|^{2}$$

In which :

$$\begin{split} E_{ke} &= \sum_{i} \int \psi_{i}^{*} (-\frac{\hbar^{2}}{2m_{e}} \Delta) \psi_{i} dV = \sum_{i} \frac{\hbar^{2}}{m_{e}} \frac{3}{2} \frac{1}{s_{i}^{2}} \\ E_{nuc\cdotnuc} &= \frac{1}{4\pi\varepsilon_{0}} \sum_{i < j} \frac{Z_{i} Z_{j}}{R_{ij}} \\ E_{nuc\cdotelec} &= -\sum_{i,j} Z_{i} \int \frac{\left|\psi_{j}\right|^{2}}{R_{ij}} dV = -\frac{1}{4\pi\varepsilon_{0}} \sum_{i,j} \frac{Z_{i}}{R_{ij}} \operatorname{Erf}\left(\frac{\sqrt{2}R_{ij}}{s_{i}}\right) \\ E_{elec\cdotelec} &= \sum_{i < j} \int \frac{\left|\psi_{i}\right|^{2} \left|\psi_{j}\right|^{2}}{x_{ij}} dV = \frac{1}{4\pi\varepsilon_{0}} \sum_{i < j} \frac{1}{x_{ij}} \operatorname{Erf}\left(\frac{\sqrt{2}x_{ij}}{\sqrt{s_{i}^{2} + s_{j}^{2}}}\right) \\ E_{Pauli} &= \sum_{\sigma_{i} = \sigma_{j}} E\left(\uparrow\uparrow\right)_{ij} + \sum_{\sigma_{i} \neq \sigma_{j}} E\left(\uparrow\downarrow\right)_{ij} \end{split}$$

Electron Force Field method

$$E_{Pauli} = \sum_{\sigma_i = \sigma_j} E(\uparrow\uparrow)_{ij} + \sum_{\sigma_i \neq \sigma_j} E(\uparrow\downarrow)_{ij}$$

$$\Psi_{Slater} = \frac{1}{\sqrt{2 - 2S^2}} (\phi_1(r_1)\phi_2(r_2) - \phi_2(r_1)\phi_1(r_2))$$

$$\Psi_{Hartree} = \phi_1(r_1)\phi_2(r_2)$$

$$E_{u} = \left\langle \Psi_{Slater} \left| -\frac{1}{2} \nabla^{2} \right| \Psi_{Slater} \right\rangle - \left\langle \Psi_{Hartree} \left| -\frac{1}{2} \nabla^{2} \right| \Psi_{Hartree} \right\rangle$$
$$= \frac{S^{2}}{1 - S^{2}} (t_{11} + t_{12} - \frac{2t_{12}}{S})$$

$$\Psi_{\rm VB} = \frac{1}{\sqrt{2+2S^2}} (\phi_1(r_1)\phi_2(r_2) + \phi_2(r_1)\phi_1(r_2))$$

$$\Psi_{Hartree} = \phi_1(r_1)\phi_2(r_2)$$

$$E_{g} = \left\langle \Psi_{\text{VB}} \right| - \frac{1}{2} \nabla^{2} \left| \Psi_{\text{VB}} \right\rangle - \left\langle \Psi_{\text{Hartree}} \right| - \frac{1}{2} \nabla^{2} \left| \Psi_{\text{Hartree}} \right\rangle$$
$$= \frac{S^{2}}{1 + S^{2}} \left(t_{11} + t_{12} - \frac{2t_{12}}{S} \right)$$



$$E(\uparrow\uparrow) = E_u - (1+\rho)E_g$$
$$E(\uparrow\downarrow) = \rho E_g$$



PNAS(2010)



Improved eFF with a boundary limitation at high temperature : **Constrianed eFF** (CEFF)





CEFF results are in good agreement with the recent results of LCLS experiments at Stanford.

进一步的流体计算表明, 激光效率沉积将差别 200%以上



87



Ma, Dai*, Zhao* and Yuan. Phys. Rev. Lett. 122: 015001 (2019)

Zeng and Dai*. Sci. China Phys. Mech. Astron. 63, 263011 (2020)

Carbon allotropes: Graphite and diamond

Thermodynamics: graphite is stable and diamond is metastable
 This is a very high energy barrier between them ~3.5 eV





Solid-to-solid structural phase transition

- It requires ultra high pressure (~50 GPa) and temperature (~3000 K) to turn graphite into diamond
- Diamond can transforms to graphite by heating it up to 1500 K







Nucleation mechanism for the direct graphite-to-diamond phase transition

nature materials



Graphene: a new paradigm in quantum materials

"Schrödinger fermions"

Electron metal







 $\widehat{H}=\hat{p}^2/2m^*$





$$\widehat{H} = v_F \vec{\sigma} \cdot \hat{p}$$

monolayer graphene

massive chiral fermions



 $\widehat{H} = \vec{\sigma} \cdot \hat{p}^2 / 2m^*$



bilayer graphene



Trilayer graphene: ABA and ABC stacking

- TLG has two stable structures: ABA Bernal & ABC rhombohedral
- Only a hexagon slip in the most top graphene layer
- > ABA is a semimetal, while ABC a gate-tunable semiconductor



Y. Shan et al, Science Advances (2018)

激光诱导物质结构相变

Ultrafast pulse laser also can trigger the structure transition
 Thermal mechanism: equilibrium, slow, irreversible...
 Pump mechanism: non-equilibrium, fast, reversible...



Nian et al, *Scientific reports* (2014)

激光诱导物质结构相变

Thermodynamics: ABC is metastable compared with ABA
 Light-induced ABC to ABA transformation
 Energy difference is determined by experiments and calculations



Zhang, Zhu* and Dai* et al. Light: Science & Applications 9:174 (2020).



- CEFF is limited in time and size scale
- Two-Temperature Model coupled Molecular Dynamics (TTM-MD, Duffy et.al, Norman et.al)

$$C_{e}\frac{\partial T_{e}}{\partial t} = -g_{ei}\left(T_{e} - T_{i}\right) + S\left(r, t\right)$$

$$m_i \frac{\partial v_i}{\partial t} = F_i(t) - \gamma_i v_i + \tilde{F}(t)$$

Laser energy:
$$S(t) = \frac{\rho \Delta \epsilon}{\tau_0 \sqrt{\pi}} \exp\left[-\left(\frac{t-t_0}{\tau_0}\right)^2\right]$$

[1]Duffy and Rutherford J Phys: Condens Matter, 2006, 19(1): 016207[2]Norman et al. Contrib Plasma Phys 2013, 53(2): 129-139



• Simulation cell

MD part: 73a*100a*100a (30nm Au foil, 2,920,000 atoms, FCC)

FE part : 84*1*1 (1-dimension electron temperature field)

• Timesteps: 1fs (MD),1as (FE)





Dynamic Process of ultrafast laser heating(0.2MJ/kg,45fs)

- 1. Laser energy deposition and electron-phonon energy exchange
- Highly non-equilibrium state
- Uniform heating (ballistic transport of electrons is considered)





Dynamic Process of ultrafast laser heating(0.2MJ/kg,45fs)

- 2. Lattice thermal response
- Partial stress confinement
- Periodic oscillation of pressure (propagation of stress wave)







Dynamic Process of ultrafast laser heating (0.2MJ/kg,45fs)

- 3. Melting mechanism
- Heterogeneous melting (10²~10³ps): propagation of melting front from free surface
- Homogeneous melting (~10¹ps) : nucleation and growth of liquid regions inside foil





Complete melting time (45fs, 35nm Au foil)

- 4. Complete melting time
- A threshold (0.19MJ/kg) is found to identify two different regimes
- Indicated a shorter melting time than measurements from Mo Science, 360: 1451 (2018).



激光诱导物质结构相变



R. Briggs et al. PRL 123 045701 (2019); S. M. Sharma et al. PRL 123 045702 (2019)

✓ 精确的状态方程,结构相变点的初步探测
 x 技术门槛高、成本昂贵
 x 缺乏微观结构高精度诊断及动力学过程观测





Hugoniot Relation

$$E - E_0 = (P + P_0)(1/\rho_0 - 1/\rho)/2$$



Figure 1. Constant velocity piston-generated shock transition from state 0 to state 1.

激光诱导物质结构相变

冲击压缩理论研究方法

DFT calculations

MD simulations



N A Smirnov JPCM 29 105402 (2017)

✓ 计算精确,状态方程预测准
 × 体系小,计算量大
 × 静态计算



H. W. Sheng PRB 83 134118 (2011)

× 依赖势函数(宽温度宽密度) ∨ 体系大,效率高 ∨ 动态过程,微观结构

激光drive冲击压缩金 FCC→BCC 相变

exp. by Briggs



exp. by Sharma DFT calculations

Laser-shock-wave combining with in-situ XRD experiments: Phys. Rev. Lett. 124, 235701 (2020); Phys. Rev. Lett. 123, 045702 (2019); Phys. Rev. Lett. 123, 045701 (2019); Nature Physics 15, 89 (2019); Phys. Rev. X 10, 011010 (2020).

 理论计算间的差异

 实验与理论计算差异

 不同实验间的差异

 104

激光诱导物质结构相变

Methods – Machine Learning based Potential

- Explicitly considered the electron temperature as an additional parameter
- Generate a many-body free energy surface

$$E[\{\psi_i\}, \{f_i\}] = U[\{\psi_i\}, \{f_i\}] - T \cdot S[\{f_i\}],$$
$$E(\mathbf{R}, T) = s(T)\tilde{E}(\mathbf{R}, T) = s(T)\sum_I \tilde{E}_I(\mathcal{R}_I, T)$$
$$s(T) \equiv \hat{\sigma}_{\mathbf{F}}(T) = e^b \cdot T^a$$

DFT calculations + Machine Learning \rightarrow Deep Potential



Wang H et al. 2018 Comput. Phys. Commun. 228 178–84

DP-GEN: an effective scheme for learning



Zhang L, Lin D Y, Wang H, et al. Phys. Rev. Mater. 3, 023804 (2019)

DP-GEN: an effective scheme for learning

Sampling:

Model deviation:

eV/A



激光诱导物质结构相变

Temperature [300, 15500] K Pressure [1, 350] GPa Init surface : vacuum length from 0 to 9 Angstrom)



激光诱导物质结构相变

Methods - MSST (Multi Scale Shock Technology)

Hugoniot relations:

For molecular dynamics simulation employ the Lagrangian:

$$u = v_{s} \left(1 - \frac{\rho_{0}}{\rho} \right)$$

$$p - p_{0} = v_{s}^{2} p_{0} \left(1 - \frac{\rho_{0}}{\rho} \right)$$

$$e - e_{0} = p_{0} \left(\frac{1}{\rho_{0}} - \frac{1}{\rho} \right) + \frac{v_{s}^{2}}{2} \left(1 - \frac{\rho_{0}}{\rho} \right)^{2}$$

 $L = T\left(\left\{\dot{\vec{r}}_{i}\right\}\right) - V\left(\left\{\vec{r}_{i}\right\}\right) + \frac{1}{2}Q\dot{\upsilon}^{2} + \frac{1}{2}\frac{v_{s}^{2}}{v_{s}^{2}}\left(\upsilon_{0} - \upsilon\right)^{2} + p_{0}(\upsilon_{0} - \upsilon)$

 $\rightarrow Q\ddot{\upsilon} = \frac{\partial T}{\partial \upsilon} - \frac{\partial V}{\partial \upsilon} - p_0 - \frac{\mathbf{v}_s^2}{\upsilon_0^2} (\upsilon_0 - \upsilon)$ where $v = \frac{1}{2}$ **Q** is a masslike parameter

Define shock speed v_s

Initial state:

 p_0, ρ_0, e_0

simulation

Hugoniot relations constraint

Molecular dynamics ____ Time-independent steady state at the shock speed **Output:** $p, \rho, e, u, T ...$

Evan J. Reed. et al. PRL, 2003, 90(23).
Dependence of Potentials



Method	Atoms	Hugoniot	Structure
Deep Potential	10000	√	\checkmark
EAM Potential	10000	×	√
DFT-MSST	96	\checkmark	× 109

Validation in NEMD Simulations



Structural Transformation



Free Energy Calculations



112

Effect of atomic defects

Effect of spherical defects











初始结构中含有缺陷会形成界面,增加界面能垒,降低内部应力,导致相变压力升高

■ 无序结构 vs 缺陷的竞争机制共同决定了FCC→BCC相变压力

Chen, Dai* et al. arXiv:2006.13136



National University of Defense Technology

Thanks for your attention!