### "材料与能源前沿科学:非平衡态物理和计算方法"培训班

# 非平衡载流子的弛豫机制

杨威

Email: wei.yang@iphy.ac.cn 中国科学院物理研究所

北京计算科学研究中心, 2020/11/12



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- 1. 介观体系的热力学平衡与非平衡
- 2. 低维体系的非平衡载流子的产生和探测
- 3. 什么是噪音谱学
- 4. GHz 噪音谱学与高电场输运的研究
- 5. 碳管布朗运动与受限量子输运的关联



热力学平衡

(equilibrium thermodynamics)

不受外界影响下,宏观性质是平衡的 (in balance),不随时间变化的状态

### 热力学非平衡

(Non-equilibrium thermodynamics)

宏观性质是非平衡	(out of balance)	,	随时间变化
的状态			



### 从经典热力学到固态量子/介观器件



### 介观 (Mesoscopic system) 纳米-微米尺度



#### **Electrons in lattices**

## 介观体系的热力学描述



温度是描述微观体系的一个很直观和具有物理量

E

### 低维系统的电学输运测量





Rev. Mod. Phy. 81, 109 (2009)





结构与物性的调控





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0 D

C60

Liang, Nature 2002



C. Urgell, Wei Yang# et al., Nature Physics 2020





C. Marcus, Science 2016

1 D

Single molecular nanotube nanowire, Si, InAs

2 D Graphene,TMD, GaAs/AlGaAs...



EPFL, 2018

3 D GaAs, GaN,Si...

### 量子点卡诺循环热机



Nature Nano. 13, 920(2018)

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## 非平衡载流子的产生-电



## 非平衡载流子的产生-光



## 非平衡载流子的产生-高电场下的Zener效应



## 电子的弛豫时间

J=0E, D= EE  $\frac{dP}{P} = -\frac{\sigma}{\epsilon}dt$  $\nabla \cdot \vec{j} + \frac{d\rho}{dt} = 0$  $\nabla \cdot D = \nabla \cdot (\overline{\tau} E) = P$  $\Rightarrow P(t) = Bexp(-\frac{t}{2})$ e 电子的强制的行机

## 电子的散射和弛豫



## 从低电场到高电场的电子输运

jsnt=nevsat it this . group velocity V 23 j=nev = neuE 高电场下, V(E)  $\mathcal{V} = \frac{\mathcal{M}\mathcal{E}}{1 + \frac{\mathcal{M}\mathcal{E}}{1 + \frac{2}{1 + 1}}^{2}}$  $V_{\text{sot}} = \frac{2}{\pi} \cdot \frac{h\Omega}{\hbar k_{\text{F}}}$ Vsat ) 广场和事场

## 非平衡载流子弛豫的探测-热输运



Grenoble, Nature Com. 2018

Suspended SiN-1D phonon waveguide 北京计算科学研究中心, 2020/11/12

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*T* (K)

## 非平衡载流子弛豫的探测-光电流



Graham et al. Nat Phys. 2013

## 非平衡载流子弛豫的探测-光+噪音



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## 非平衡载流子弛豫的探测--纳米机械学



## 非平衡载流子弛豫的探测-噪音谱学



Bernard Placais, PRL 2012 & Nature Physics 2013



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测量与噪音





measured signal is fluctuating in time



 $I(t) = <l > +\delta I(t)$ 

 $S_{II} = \delta I^2 / f$ 



噪音的种类



Alexander A. Balandin, Nat. Nano. 8, 549 (2013).



Resonances RLC Vibration Microwave Cavity

 $S_{total} = \alpha_H V^2 / Nf + S_V$ 

thermal noise shot noise

...



 $S_I = F * 2eI$ 

噪音与电子输运特性-Fano factor



噪音谱学的应用



#### Ground state cooling



#### Electron pairing in LaSrCuO junction



Nature 572,493 (2019)

GHz噪音谱的标定



$$\mathbf{S}_{VV}^{out} = \mathbf{S}_{VV}^{sample} + \mathbf{S}_{VV}^{amp.line}$$

A tunnel junction is used to  
calibrate the background noise  
$$\mathbf{S}_{VV}^{sample} = \mathbf{S}_{VV}^{TJ} \propto 2e \mathbf{I}_{ds} \longrightarrow \mathbf{I}_{noise}$$



Noise spectra with a bandwidth of ~5 GHz

热噪音与电子温度

Noise temperature  $k_B T_N \equiv S_I / 4G_{diff}$ 电子温度 Hot electrons, heat equation, Wiedemann-Frantz  $k_B T_N \equiv \langle k_B T_e \rangle = \frac{\sqrt{3}}{8} \times Length \times \sqrt{P/\sigma}$  $k_B T_e$ 电子-空穴对 Hot Fermi sea + holes  $k_B T_N \equiv \int_{-\infty}^{\infty} f(1-f) dE \approx k_B T_e + \frac{n_h}{DOS}$ FK = JoT Charge + heat  $L_{o} = \frac{\pi^{2}}{2} \left(\frac{k_{s}}{2}\right)^{2}$ 

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## 石墨烯的能带和声子谱









### Weak electron-phonon coupling

#### Weak thermal electron-phonon coupling

$$P(T \ll \theta_{BG}) = \Sigma \Delta T^{4} = \frac{\pi^{2} D^{2} k_{B}^{4} |\mu|}{15 \rho_{m} \hbar^{5} s^{3} v_{F}^{3}} \times (T_{e}^{4} - T_{ph}^{4})$$
$$P(T \gg \theta_{BG}) = G_{o} \Delta T = \frac{D^{2} k_{B} |\mu|^{4}}{2 \pi \rho_{m} \hbar^{5} v_{F}^{6}} \times (T_{e} - T_{ph})$$

J. K. Viljas and T. T. Heikkilä PRB (2010)



### 电子-声子弛豫的三种常见类型



$$-\frac{\sigma\pi^{2}L^{2}}{6}\frac{\partial^{2}}{\partial x^{2}}\left(\frac{k_{B}T_{e}}{e}\right) = \varepsilon \cdot J - P(T_{e}, T_{ph}) - P_{OP}$$

$$\frac{WF}{6}\frac{Low-TAC}{6}\frac{Super-collisions}{Collisions} OP$$

$$\frac{P \propto T^{2}}{2}\frac{\alpha T^{3}}{\alpha T^{4}}\frac{\alpha exp[T/\Omega_{OP}]}{\alpha T^{2}}$$

$$\frac{WF}{6}\frac{WF$$



### 迁移率对器件的影响



## 高质量G/hBN器件









### **Hyperbolic phonons of hBN**



*(Courtesy of F. Koppens, Kaprun School 2015)* 北京计算科学研究中心, 2020/11/12

## G/hBN 的高电场输运特性



### **Zener-Klein tunneling**



Wei Yang, et al. Nature Nano. 13, 47(2018)

Zener-Klein Tunneling, Pauli blocking:  

$$\sigma_{ZK} = \alpha \frac{4e^2}{h} \frac{k_F l_{ZK}}{4\pi} = Const. \quad ; \quad \dot{n}_{e-h}^{ZK} = \frac{e k_F}{\pi^2 \hbar} (E - E_{ZK})$$

$$E_{zk} = \frac{2E_F}{el_{zk}} \text{ (dashed line)}$$

## 低电场下的电流饱和效应



### 器件的直流测量与GHz 热噪音测量



### **Zener Klein tunneling and Hyperbolic cooling**



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### **ZK and HPP at CNP**



### ZK and HPP at medium doping



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### Hot electrons and HPP emissions at high doping



Super-Planck HPP thermal emission  $(\sigma_{hot}(\omega, q) \text{ by Polini at al.})$   $P_J = 0.5 \frac{GW}{m^2}, \ kT = 0.4 eV, \ n_e = 4 \ 10^{12}$  $\swarrow P_{HPP}^{th} = 2.4 \times M \ \frac{GW}{m^2} = 0.24 \ \frac{GW}{m^2} = P_J/2 = P_{WF}$  by taking  $M^{th} \approx 0.1$ 

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#### Bilayer graphene in magnetic field



Zener field  $E_c \sim \hbar \omega_c / e R_c$   $\omega_c = e B / m^*$ ( $R_c \sim \sqrt{N} l_B$   $l_B = \sqrt{\hbar / e B}$ )

#### Two probe measurement of QHE in BLG



Wei Yang et al, PRL.121, 136804 (2018).

#### Quantum Hall breakdown captured by noise avalanche



#### Many-Body interaction induced QHE breakdown





S<sub>I</sub>=Fano\*2el<sub>ds</sub>



Wei Yang et al, PRL.121, 136804 (2018).



- 发现了Zener-Klein隧穿效应,揭示了非平衡电子-空 穴对的存在
- 实现一种远程声子辅助的高效制冷,解决了电子器 件高功率工作下热力学不稳定的问题
- 首次观测到量子霍尔效应的崩溃临界电场与本征齐 纳临界电场吻合
- 提出一种磁激发不稳定引发量子霍尔效应崩溃的新机制,打破了长期采用单电子图像描述的局限性

[1] <u>Wei Yang</u>, et al. Nature Nanotechnology, 13, 47 (2018).

[2] <u>Wei Yang</u>, et al. Phy. Rev. Lett., 121, 136804 (2018).

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#### Mechanical resonators



M. Poggio et al. PRL (2007)



Cleland Group, Nature (2009)



A. Naik et al. Nature (2006)

by Side band cooling

J. D. Teufel al. Nature (2011)

2 μm Ground state



J. D. Thompson et al. Nature (2008)





Kippenberg Group, Nature (2007)

S CNT D Gate

### CNT for sensing applications

#### Mass sensing with yg (10<sup>-24</sup>g) resolution





Bachtold's Group Nature Nano. 7, 301 (2012)

$$f = \sqrt{k/m}$$

Force sensitivity of ~12  $zN/\sqrt{Hz}$ 



Bachtold's Group Nature Nano. 8, 493 (2012)

 $S_{\rm F} = 4k_{\rm B}T\gamma = 4k_{\rm B}T\sqrt{Mk_0/Q}$ 

#### Basics about quantum transport in CNT



### **Coulomb Blockade**

 $k_B T, \Gamma \ll E_C$  $R > h/e^2$ 



#### **Coulomb Blockade**



#### Kondo resonance



#### Zero bias conductance Kondo ridge



#### Transparent tunnelling *Fabry perot Interference*



$$L = \frac{hv_f}{2eV_c} = 1.22 \ \mu m$$





#### Detection of the nanotube's vibration



C.Urgell#, W. Yang#\*, et al. Nature Physics 16, 32(2020)

Adrian Bachtold Carles Urgell



$$\int_{-\infty}^{+\infty} S_{xx}(\omega) \frac{d\omega}{2\pi} = \langle x^2 \rangle.$$

$$m\omega_0^2 \langle x \rangle^2 = k_B T$$

sample



#### Ultra-clean CNT Resonator, also a good transistor

北京计算科学研究中心, 2020/11/12

#### **Dynamic heating and Self-Oscillations**



#### The measured voltage signal



#### The extracted vibration motion





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#### Dynamic cooling the resonator to a state of few quanta



#### **Electrothermal model**



结





- 实现了高灵敏度的 MHz噪音测量(0.5 pm/√Hz)
- 实现了电子对碳管热振动的量子反作用调控
- 实现将谐振子冷却到接近量子基态(~4.6 量子)

[1] C. Urgell#, <u>W. Yang</u>#\*, et al. Nature Physics, 16, 32 (2020).
[2] S. L. de Bonis#, C. Urgell#, <u>W. Yang</u>, et al. Nano Letters, 18, 5324 (2018).

## What Now?.....

### Multilayer Van de Waals Devices

Multilayer MoS<sub>2</sub> FETs





Jian Tang, et al., Advanced Electronic Materials, 2000550(2020)

### Moir éPhysics-From single particle to many body interaction







### THERE IS PLENTY OF ROOM AT THE BOTTOM

---Richard Feynman



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ICFO<sup>9</sup> erc

Carles Urgell

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欢迎交流、加入我们!

杨威,特聘研究员

物理所-纳米实验室N07组

Email: wei.yang@iphy.ac.cn

**Tel:** 010-82648050

http://www.iop.cas.cn/rcjy/yjdwfgj/?id=1349

Thanks very much!